Welcome to the digital design lab! Today’s task is to build a half-adder and a full-adder.

1 Knowing what the toys are

Don’t do anything yet! We’re going to spend a few minutes going over the various chips, boards, power supplies, and other devices that you’ll need to use for this and other labs. Here’s a list of the devices you’ll be using, and some key information about them:

- **Breadboard and the ETS-7000**: These big units have a number of parts, some of which we’ll never use. Their key feature is the **breadboard**—white boards with lots of little holes in them. These will allow us to structure our circuits, as we’ll have to plug all of the chips and wires into them to make them work. Each breadboard has **power and ground channels** that provide the digital zeros (0 volts) and ones (+5 volts) that we will use as inputs into gates. More on these below. The breadboard also has **wells** that chips straddle, with independent rows of connected holes that allow you to connect a wire to a chip pin by putting that wire in the same row.

Note that the ETS-7000 also contain a number of devices around the periphery for input and output. For now, we are interested in the eight **switches** at the bottom that allow us to easily select power and ground inputs; we are also going to use the eight **LEDs** in the upper-right corner, allowing us to see the value flowing out of our circuits.

- **Power channels**: There are several power channels on each board, marked by red or blue/black lines. The colors respectively mean power and ground. There should be wires from the posts to two of the power channels. Each power channel is electrically connected inside the board, meaning that once a channel is connected to a source (in the upper left corner of the ETS-7000), power is available at each post in the channel. There should be wires connecting all of the red channels together and all of the blue/black channels together. If these wires are not already on your board, you can add them as you go. **Again, don’t get red and black reversed.**

- **Chips**: We’ll use three kinds of chips today: 7404 (**NOT** gates), 7408 (**AND** gates), and 7432 (**OR** gates). Data sheets describing the operation of these chips are attached. As the semester goes on, you’ll be using lots of other chips. Data books on the shelf in the lab describe their operation. When possible, data sheets will also be posted on the class web pages, under the **Documents** section. Some important notes on the chips and their use:

  - **Orientation**: Each chip has a mark, either a small hole or a small cutout, to indicate the top end. The top pin on the left is pin 1. The pin numbers go down the left side and up the right side. Most of our chips have 14 pins, but some will have more.

  - **Power and ground pins**: Two pins on each chip must be connected to power channels. The pin marked $V_{cc}$ on the data sheet should be connected to the red channel. The pin marked $GND$ should be connected to the black/blue channel. **Don’t get them backwards, and don’t install the chip upside down.**
– **Installing chips:** Chips must be laid on the board with the right end up and with the pins straddling the groove. Each row of five pins is electrically connected within the board. By placing the chip so it straddles the groove, you are ensuring that there are separate sets of holes for each pin of the chip. Be sure to press each chip in gently and evenly, without letting one end or the other twist up or down. This will help you avoid breaking pins.

– **Removing chips:** Remove chips carefully and evenly, by using a chip extractor and pulling straight up. Do not try to remove the chips with your fingers, as you’ll probably bend or break the pins in the process. Return each chip to the place you got it.

- **Wires:** There are bins of wires available for your use, as well as kits that contain pre-cut, pre-bent wires that are color-coded by length. When you make a connection on the board, try to do it neatly and try to avoid using wires that are too long for the purpose. Your work will be far easier to test and correct if the wires are short, well organized, and labeled. When you need a wire of a certain length, you can either look for one or you can make one from a longer wire, using wire strippers to cut and remove insulation. You may even want to devise for yourself a wire-color scheme, such that each color implies something about the purpose to which the wire is being put.

- **Logic probes:** Logic probes are great debugging tools. If you connect them to power you can insert the probe tip into holes to determine if there is a positive voltage (a red light and a high-pitched sound), a ground connection (a green light and a low-pitched sound), or an open connection (no light or sound). *Probes don’t always work in locations that are connected to LEDs.* As an alternative, you can always use a wire connected to one of the ETS-7000’s LEDs as an ad-hoc logic probe.

We may not use all of these parts in the first lab, but you will need a number of them, and eventually you will use all of them and more.

## 2 What to build

It is unwise to construct a complete solution without testing its parts along the way. With a large circuit, you want first to construct the smaller circuits that will later compose the large one. With each smaller circuit, you should debug it thoroughly before connecting it to other smaller circuits. That way, you can have some confidence that certain portions of your larger circuit work correctly, reducing the number of possible portions of your circuit that may be designed or constructed in error.

### 2.1 Half-adder

We begin with by constructing a half-adder. Since this circuit is our first, you can follow these instructions to construct it and become familiar with the components involved:

1. Set up a single AND gate by using a 7408 chip. Set up an LED so that you can see the output of this gate. Try all four possible inputs to be sure that it’s operating correctly. You’ve just
constructed the circuit the generate the carry bit for your half-adder, where one input is your $a$ value, and the other your $b$ value.

2. Begin constructing an XOR circuit by using the NOT gates in the 7404 chip. You will want use two gates, one to produce $\overline{a}$, and the other to produce $\overline{b}$.

3. Use two more of the AND gates from the same 7408 chip as you used above. To one gate, connect $a$ and $\overline{b}$, and to the other $\overline{a}$ and $b$.

4. Finally, bring the outputs of the two AND gates used in the previous step, and connect them as inputs to an OR gate on your 7432 chip. The output of this particular gate is $a \oplus b$, also known as the result bit.

5. Wire the outputs of these two circuits so that they appear adjacent to other another on an LED. Once you’ve done that, you have a half-adder!

### 2.2 Full-adder

Now that you have constructed a half-adder, use another part of your board to construct a full-adder. That is, you need to devise an adder than can sum three 1-bit values. This device is useful because it can add not only the two bits of some value, but also a third bit that can be considered the carry value from a less significant 3-bit addition. That is, a full-adder is capable of adding the bits in one column of significance in a larger addition problem. Thus, this device will have $a$, $b$, and $c_i$ inputs, where the third is the carry-in value. Likewise, you will find that there are two output bits, $r$ (for result) and $c_o$ (for carry-out).

To perform this task, you should:

1. Lay out a truth table that enumerates the possible input values for $a$, $b$, and $c_i$. Notice that with 3 inputs, there are $2^3 = 8$ combinations of input values. Therefore, your truth table should contain the 8 entries that enumerate all of the possible input values, and then list the correct output values.

2. Define the outputs ($r$ and $c_o$) in terms of the inputs ($a$, $b$, and $c_i$). If you have never worked with logic functions before, you should ask for help—I don’t expect you yet to define these functions with ease merely by looking at the truth table.

3. Draw circuits that implement $r$ and $c_o$.

4. Build the circuits that you’ve drawn. Evaluate your work by testing every possible combination of inputs, determining that the outputs generated by your circuit match those shown in your truth table.

### 3 Finishing up / Demonstrating your work

Every week, there are some things you’ll have to do whether or not you’ve completed the assignment.
1. **Demonstrating your work:** If you’ve finished the lab, then you need to show it to the professor or the TA. **You won’t get credit unless we’ve seen it work!** Be sure to show both the half-adder and the full-adder. If you do not complete the lab by the end of the lab session (a likely a common occurrence), then you can show your work later in the week, before the next lab.

2. **Saving your work for another day:** First, be sure to label your ETS-7000; **Unlabeled work may be dismantled!** You need not put it away, since we lack the shelving to have everyone put theirs into storage. However, someone may reasonably move your ETS-7000 during the week. If you move someone else’s, please do so carefully.

3. **Cleaning up:** When you’re done, put away everything and clean up your area. That is, clean up the little bits of wire and insulation, put away the tools, etc. Leave a clean workspace, or else this lab will be a disaster before long, making it a difficult place in which to get work done.

**[Extended deadline] This assignment is due at on Monday, Sep-16.**